

## NAG C Library Function Document

### nag\_complex\_sparse\_eigensystem\_iter (f12apc)

#### 1 Purpose

nag\_complex\_sparse\_eigensystem\_iter (f12apc) is an iterative solver in a suite of functions consisting of nag\_complex\_sparse\_eigensystem\_iter (f12apc), nag\_complex\_sparse\_eigensystem\_init (f12anc), nag\_complex\_sparse\_eigensystem\_sol (f12aqc), nag\_complex\_sparse\_eigensystem\_option (f12arc) and nag\_complex\_sparse\_eigensystem\_monit (f12asc). It is used to find some of the eigenvalues (and optionally the corresponding eigenvectors) of a standard or generalized eigenvalue problem defined by complex non-symmetric matrices.

#### 2 Specification

```
#include <nag.h>
#include <nagf12.h>
```

```
void nag_complex_sparse_eigensystem_iter (Integer *irevcn, Complex resid[],
    Complex v[], Complex **x, Complex **y, Complex **mx, Integer *nshift,
    Complex comm[], Integer icomm[], NagError *fail)
```

#### 3 Description

The suite of functions is designed to calculate some of the eigenvalues,  $\lambda$ , (and optionally the corresponding eigenvectors,  $x$ ) of a standard eigenvalue problem  $Ax = \lambda x$ , or of a generalized eigenvalue problem  $Ax = \lambda Bx$  of order  $n$ , where  $n$  is large and the coefficient matrices  $A$  and  $B$  are sparse, complex and non-symmetric. The suite can also be used to find selected eigenvalues/eigenvectors of smaller scale dense, complex and non-symmetric problems.

nag\_complex\_sparse\_eigensystem\_iter (f12apc) is a **reverse communication** function, based on the ARPACK routine **znaupd**, using the Implicitly Restarted Arnoldi iteration method. The method is described in Lehoucq and Sorensen (1996) and Lehoucq (2001) while its use within the ARPACK software is described in great detail in Lehoucq *et al.* (1998). An evaluation of software for computing eigenvalues of sparse non-symmetric matrices is provided in Lehoucq and Scott (1996). This suite of functions offers the same functionality as the ARPACK software for complex non-symmetric problems, but the interface design is quite different in order to make the option setting clearer to you and to simplify the interface of nag\_complex\_sparse\_eigensystem\_iter (f12apc).

The setup function nag\_complex\_sparse\_eigensystem\_init (f12anc) must be called before nag\_complex\_sparse\_eigensystem\_iter (f12apc), the reverse communication iterative solver. Options may be set for nag\_complex\_sparse\_eigensystem\_iter (f12apc) by prior calls to the option setting function nag\_complex\_sparse\_eigensystem\_option (f12arc) and a post-processing function nag\_complex\_sparse\_eigensystem\_sol (f12aqc) must be called following a successful final exit from nag\_complex\_sparse\_eigensystem\_iter (f12apc). nag\_complex\_sparse\_eigensystem\_monit (f12asc), may be called following certain flagged, intermediate exits from nag\_complex\_sparse\_eigensystem\_iter (f12apc) to provide additional monitoring information about the computation.

nag\_complex\_sparse\_eigensystem\_iter (f12apc) uses **reverse communication**, i.e., it returns repeatedly to the calling program with the argument **irevcn** (see Section 5) set to specified values which require the calling program to carry out one of the following tasks:

- compute the matrix-vector product  $y = OPx$ , where  $OP$  is defined by the computational mode;
- compute the matrix-vector product  $y = Bx$ ;
- notify the completion of the computation;
- allow the calling program to monitor the solution.

The problem type to be solved (standard or generalized), the spectrum of eigenvalues of interest, the mode used (regular, regular inverse, shifted inverse, shifted real or shifted imaginary) and other options can all be set using the option setting function `nag_complex_sparse_eigensystem_option` (f12arc) (see Section 10.2 of the document for `nag_complex_sparse_eigensystem_option` (f12arc) for details on setting options and of the default settings).

## 4 References

Lehoucq R B (2001) Implicitly Restarted Arnoldi Methods and Subspace Iteration *SIAM Journal on Matrix Analysis and Applications* **23** 551–562

Lehoucq R B and Scott J A (1996) An evaluation of software for computing eigenvalues of sparse nonsymmetric matrices *Preprint MCS-P547-1195* Argonne National Laboratory

Lehoucq R B and Sorensen D C (1996) Deflation Techniques for an Implicitly Restarted Arnoldi Iteration *SIAM Journal on Matrix Analysis and Applications* **17** 789–821

Lehoucq R B, Sorensen D C and Yang C (1998) *ARPACK Users' Guide: Solution of Large-Scale Eigenvalue Problems with Implicitly Restarted Arnoldi Methods* SIAM, Philadelphia

## 5 Arguments

**Note:** this function uses **reverse communication**. Its use involves an initial entry, intermediate exits and re-entries, and a final exit, as indicated by the **argument irevcn**. Between intermediate exits and re-entries, **all arguments other than x and y must remain unchanged**.

1: **irevcn** – Integer \* *Input/Output*

*On initial entry:* **irevcn** = 0, otherwise an error condition will be raised.

*On intermediate re-entry:* must be unchanged from its previous exit value. Changing **irevcn** to any other value between calls will result in an error.

*On intermediate exit:* has the following meanings.

- 1 The calling program must compute the matrix-vector product  $y = OPx$ , where  $x$  is stored in **x** and the result  $y$  is placed in **y**.
  - 1 The calling program must compute the matrix-vector product  $y = OPx$ . This is similar to the case **irevcn** = –1 except that the result of the matrix-vector product  $y = Bx$  (as required in some computational modes) has already been computed and is available in **mx**.
  - 2 The calling program must compute the matrix-vector product  $y = Bx$ , where  $x$  is stored in **x** and  $y$  is placed in **y**.
  - 3 Compute the **nshift** complex shifts to be placed in the first **nshift** locations of the array **y**. This value of **irevcn** will only arise if the option **Supplied Shifts** is set in a prior call to `nag_complex_sparse_eigensystem_option` (f12arc) (see Section 10.2 of the document for `nag_complex_sparse_eigensystem_option` (f12arc)) which is intended for experienced users only; the default and recommended option is to use exact shifts (see Lehoucq *et al.* (1998) for details).
  - 4 Monitoring step: a call to `nag_complex_sparse_eigensystem_monit` (f12asc) can now be made to return the number of Arnoldi iterations, the number of converged Ritz values, the array of converged values, and the corresponding Ritz estimates.

*On final exit:* **irevcn** = 5: `nag_complex_sparse_eigensystem_iter` (f12apc) has completed its tasks. The value of **fail** determines whether the iteration has been successfully completed, or whether errors have been detected. On successful completion `nag_complex_sparse_eigensystem_sol` (f12aqc) must be called to return the requested eigenvalues and eigenvectors (and/or Schur vectors).

*Constraint:* on initial entry, **irevcn** = 0; on re-entry **irevcn** must remain unchanged.

- 2: **resid**[*dim*] – Complex *Input/Output*  
**Note:** the dimension, *dim*, of the array **resid** must be at least **n** (see `nag_complex_sparse_eigensystem_init` (f12anc)).  
*On initial entry:* need not be set unless the option **Initial Residual** has been set in a prior call to `nag_complex_sparse_eigensystem_option` (f12arc) in which case **resid** should contain an initial residual vector, possibly from a previous run.  
*On intermediate re-entry:* must be unchanged from its previous exit. Changing **resid** to any other value between calls may result in an error exit.  
*On intermediate exit:* contains the current residual vector.  
*On final exit:* contains the final residual vector.
- 3: **v**[*dim*] – Complex *Input/Output*  
**Note:** the dimension, *dim*, of the array **v** must be at least  $\max(1, \mathbf{ncv})$  (see `nag_complex_sparse_eigensystem_init` (f12anc)).  
The *i*th element of the *j*th basis vector is stored in location  $\mathbf{v}[j \times \mathbf{n} + i]$ , for  $i = 0, 1, \dots, \mathbf{n} - 1$  and  $j = 0, 1, \dots, \mathbf{ncv} - 1$ .  
*On initial entry:* need not be set.  
*On intermediate re-entry:* must be unchanged from its previous exit.  
*On intermediate exit:* contains the current set of Arnoldi basis vectors.  
*On final exit:* contains the final set of Arnoldi basis vectors.
- 4: **x** – Complex \*\* *Output*  
*On initial entry:* need not be set, it is used as a convenient mechanism for accessing elements of **comm**.  
*On intermediate re-entry:* is not normally changed.  
*On intermediate exit:* contains the vector *x* when **irevcn** returns the value  $-1$ ,  $+1$  or  $2$ .  
*On final exit:* does not contain useful data.
- 5: **y** – Complex \*\* *Input/Output*  
*On initial entry:* need not be set, it is used as a convenient mechanism for accessing elements of **comm**.  
*On intermediate re-entry:* must contain the result of  $y = OPx$  when **irevcn** returns the value  $-1$  or  $+1$ . It must contain the computed shifts when **irevcn** returns the value  $3$ .  
*On intermediate exit:* does not contain useful data.  
*On final exit:* does not contain useful data.
- 6: **mx** – Complex \*\* *Output*  
*On initial entry:* need not be set, it is used as a convenient mechanism for accessing elements of **comm**.  
*On intermediate re-entry:* must contain the result of  $y = Bx$  when **irevcn** returns the value  $2$ .  
*On intermediate exit:* contains the vector *Bx* when **irevcn** returns the value  $+1$ .  
*On final exit:* does not contain any useful data.
- 7: **nshift** – Integer \* *Output*  
*On intermediate exit:* if the option **Supplied Shifts** is set and **irevcn** returns a value of  $3$ , **nshift** returns the number of complex shifts required.

- 8: **comm**[*dim*] – Complex *Communication Array*  
**Note:** the dimension, *dim*, of the array **comm** must be at least  $\max(1, 3 \times \mathbf{n} + 3 \times \mathbf{ncv} \times \mathbf{ncv} + 5 \times \mathbf{ncv} + 60)$  (see `nag_complex_sparse_eigensystem_init` (f12anc)).  
*On initial entry:* must remain unchanged following a call to the setup function `nag_complex_sparse_eigensystem_init` (f12anc).  
*On exit:* contains data defining the current state of the iterative process.
- 9: **icomm**[*dim*] – Integer *Communication Array*  
**Note:** the dimension, *dim*, of the array **icomm** must be at least  $\max(1, \mathbf{licomm})$  (see `nag_complex_sparse_eigensystem_init` (f12anc)).  
*On initial entry:* must remain unchanged following a call to the setup function `nag_complex_sparse_eigensystem_init` (f12anc).  
*On exit:* contains data defining the current state of the iterative process.
- 10: **fail** – NagError \* *Input/Output*  
The NAG error argument (see Section 2.6 of the Essential Introduction).

## 6 Error Indicators and Warnings

### NE\_ALLOC\_FAIL

Error: unable to allocate requested internal workspace.

### NE\_BAD\_PARAM

On entry, argument *<value>* had an illegal value.

### NE\_INITIALIZATION

Either the initialization function has not been called prior to the first call of this function or a communication array has become corrupted.

### NE\_INT

The maximum number of iterations  $\leq 0$ , the option **Iteration Limit** has been set to *<value>*.

### NE\_INTERNAL\_EIGVAL\_FAIL

Error in internal call to compute eigenvalues and corresponding error bounds of the current upper Hessenberg matrix. Please contact NAG.

### NE\_INTERNAL\_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please consult NAG for assistance.

### NE\_MAX\_ITER

The maximum number of iterations has been reached. The maximum number of iterations = *<value>*. The number of converged eigenvalues = *<value>*. The post-processing function `nag_complex_sparse_eigensystem_sol` (f12aqc) may be called to recover the converged eigenvalues at this point. Alternatively, the maximum number of iterations may be increased by a call to the option setting function `nag_complex_sparse_eigensystem_option` (f12arc) and the reverse communication loop restarted. A large number of iterations may indicate a poor choice for the values of **ncv** and **ncv**; it is advisable to experiment with these values to reduce the number of iterations (see `nag_complex_sparse_eigensystem_init` (f12anc)).

**NE\_NO\_ARNOLDI\_FAC**

Could not build an Arnoldi factorization. The size of the current Arnoldi factorization =  $\langle value \rangle$ .

**NE\_NO\_SHIFTS\_APPLIED**

No shifts could be applied during a cycle of the implicitly restarted Arnoldi iteration.

**NE\_OPT\_INCOMPAT**

The options **Generalized** and **Regular** are incompatible.

**NE\_ZERO\_INIT\_RESID**

The option **Initial Residual** was selected but the starting vector held in **resid** is zero.

**7 Accuracy**

The relative accuracy of a Ritz value,  $\lambda$ , is considered acceptable if its Ritz estimate  $\leq \mathbf{Tolerance} \times |\lambda|$ . The default **Tolerance** used is the *machine precision* given by `nag_machine_precision (X02AJC)`.

**8 Further Comments**

None.

**9 Example**

The example solves  $Ax = \lambda x$  in shift-invert mode, where  $A$  is obtained from the standard central difference discretization of the convection-diffusion operator  $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \rho \frac{\partial u}{\partial x}$  on the unit square, with zero Dirichlet boundary conditions. The shift used is a complex number.

**9.1 Program Text**

```

/* nag_complex_sparse_eigensystem_iter (f12apc) Example Program.
 *
 * Copyright 2005 Numerical Algorithms Group.
 *
 * Mark 8, 2005.
 */

#include <math.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nag_string.h>
#include <stdio.h>
#include <naga02.h>
#include <nagf12.h>
#include <nagf16.h>
static void my_zgttrf(Integer, Complex *, Complex *, Complex *,
                    Complex *, Integer *, Integer *);
static void my_zgttrs(Integer, Complex *, Complex *, Complex *,
                    Complex *, Integer *, Complex *, Complex *);

int main(void)
{
    /* Constants */
    Integer licomm=140, imon=0;

    /* Scalars */
    Complex rho, s1, s2, s3, sigma;
    double  estnrm, hr1, hr2, sr;
    Integer exit_status, info, irevcm, j, lcomm, n, nconv;
    Integer ncv, nev, niter, nshift, nx;
    /* Nag types */

```

```

NagError fail;
/* Arrays */
Complex *comm=0, *eigv=0, *eigest=0, *dd=0, *dl=0, *du=0;
Complex *du2=0, *resid=0, *v=0;
Integer *icomm=0, *ipiv=0;
/* Ponters */
Complex *mx=0, *x=0, *y=0;

exit_status = 0;
INIT_FAIL(fail);

Vprintf("nag_complex_sparse_eigensystem_iter (f12apc) Example Program "
        "Results\n");
/* Skip heading in data file */
Vscanf("%*[\n] ");

Vscanf("%ld%ld%ld%*[\n] ", &nx, &nev, &ncv);
n = nx * nx;
lcomm = 3*n + 3*ncv*ncv + 5*ncv + 60;
/* Allocate memory */
if ( !(comm = NAG_ALLOC(lcomm, Complex)) ||
      !(eigv = NAG_ALLOC(ncv, Complex)) ||
      !(eigest = NAG_ALLOC(ncv, Complex)) ||
      !(dd = NAG_ALLOC(n, Complex)) ||
      !(dl = NAG_ALLOC(n, Complex)) ||
      !(du = NAG_ALLOC(n, Complex)) ||
      !(du2 = NAG_ALLOC(n, Complex)) ||
      !(resid = NAG_ALLOC(n, Complex)) ||
      !(v = NAG_ALLOC(n * ncv, Complex)) ||
      !(icomm = NAG_ALLOC(lcomm, Integer)) ||
      !(ipiv = NAG_ALLOC(n, Integer)) )
    {
    Vprintf("Allocation failure\n");
    exit_status = -1;
    goto END;
    }
/* Initialise communication arrays for problem using
   nag_complex_sparse_eigensystem_init (f12anc). */
nag_complex_sparse_eigensystem_init(n, nev, ncv, icomm, lcomm,
                                     comm, lcomm, &fail);
/* Select the required mode using
   nag_complex_sparse_eigensystem_option (f12arc). */
nag_complex_sparse_eigensystem_option("SHIFTED INVERSE", icomm,
                                       comm, &fail);
/* Set values for sigma and rho */
/* Assign to Complex type using nag_complex (a02bac) */
sigma = nag_complex(0.0, 0.0);
rho = nag_complex(10.0, 0.0);
hr1 = (double) (n+1);          /* 1/h */
hr2 = hr1*hr1;                 /* 1/(h*h) */
sr = 0.5*hr1*rho.re;          /* s/h */
/* Assign to Complex type using nag_complex (a02bac) */
s1 = nag_complex(-hr2-sr,0.0); /* -1/(h*h) - s/h */
s3 = nag_complex(-hr2+sr,0.0); /* -1/(h*h) + s/h */
s2 = nag_complex(2.0*hr2,0.0);
/* Compute Complex subtraction using nag_complex_subtract
   (a02cbc). */
s2 = nag_complex_subtract(s2,sigma); /* two/(h*h) - sigma */

for (j = 0; j <= n - 2; ++j)
    {
    dl[j] = s1;
    dd[j] = s2;
    du[j] = s3;
    }
dd[n - 1] = s2;

my_zgtrf(n, dl, dd, du, du2, ipiv, &info);
irevcm = 0;
REVCOMLOOP:
/* repeated calls to reverse communication routine

```

```

    nag_complex_sparse_eigensystem_iter (f12apc). */
nag_complex_sparse_eigensystem_iter(&irevcm, resid, v, &x, &y, &mx,
                                     &nshift, comm, icomm, &fail);
if (irevcm != 5)
{
    if (irevcm == -1 || irevcm == 1)
    {
        /* Perform  $x \leftarrow OP*x = \text{inv}[A-\sigma I]*x$  */
        my_zgttrs(n, dl, dd, du, du2, ipiv, x, y);
    }
    else if (irevcm == 4 && imon == 1)
    {
        /* If imon=1, get monitoring information using
           nag_complex_sparse_eigensystem_monit (f12asc). */
        nag_complex_sparse_eigensystem_monit(&niter, &nconv, eigv,
                                             eigest, icomm, comm);

        /* Compute 2-norm of Ritz estimates using
           nag_zge_norm (f16uac). */
        nag_zge_norm(Nag_ColMajor, Nag_FrobeniusNorm, nev, 1, eigest,
                    nev, &estnrm, &fail);
        Vprintf("Iteration %3ld, ", niter);
        Vprintf(" No. converged = %3ld,", nconv);
        Vprintf(" norm of estimates = %16.8e\n\n", estnrm);
    }
    goto REVCOMLOOP;
}
if (fail.code == NE_NOERROR)
{
    /* Post-Process using nag_complex_sparse_eigensystem_sol
       (f12aqc) to compute eigenvalues/vectors. */
    nag_complex_sparse_eigensystem_sol(&nconv, eigv, v, sigma,
                                       resid, v, comm, icomm,
                                       &fail);

    Vprintf("\n");
    Vprintf(" The %4ld Ritz values of smallest magnitude are:\n\n",
            nconv);
    for (j = 0; j <= nconv-1; ++j)
    {
        Vprintf("%8ld%5s( %12.4f , %12.4f )\n", j+1, "",
                eigv[j].re, eigv[j].im);
    }
}
else
{
    Vprintf(" Error from nag_complex_sparse_eigensystem_iter (f12apc). "
           "\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}
END:
if (comm) NAG_FREE(comm);
if (eigv) NAG_FREE(eigv);
if (eigest) NAG_FREE(eigest);
if (dd) NAG_FREE(dd);
if (dl) NAG_FREE(dl);
if (du) NAG_FREE(du);
if (du2) NAG_FREE(du2);
if (resid) NAG_FREE(resid);
if (v) NAG_FREE(v);
if (icomm) NAG_FREE(icomm);
if (ipiv) NAG_FREE(ipiv);

return exit_status;
}

static void my_zgttrf(Integer n, Complex dl[], Complex d[],
                    Complex du[], Complex du2[], Integer ipiv[],
                    Integer *info)
{
    /* A simple C version of the Lapack routine zgttrf with argument
       checking removed */

```

```

/* Scalars */
Complex temp, fact, z1;
Integer i;
/* Function Body */
*info = 0;
for (i = 0; i < n; ++i)
{
    ipiv[i] = i;
}
for (i = 0; i < n - 2; ++i)
{
    du2[i] = nag_complex(0.0,0.0);
}
for (i = 0; i < n - 2; ++i)
{
    if (fabs(d[i].re)+fabs(d[i].im) >= fabs(dl[i].re)+fabs(dl[i].im))
    {
        /* No row interchange required, eliminate dl[i]. */
        if (fabs(d[i].re)+fabs(d[i].im) != 0.0)
        {
            /* Compute Complex division using nag_complex_divide
            (a02cdc). */
            fact = nag_complex_divide(dl[i],d[i]);
            dl[i] = fact;
            /* Compute Complex multiply using nag_complex_multiply
            (a02ccc). */
            fact = nag_complex_multiply(fact,du[i]);
            /* Compute Complex subtraction using
            nag_complex_subtract (a02cbc). */
            d[i+1] = nag_complex_subtract(d[i+1],fact);
        }
    }
    else
    {
        /* Interchange rows I and I+1, eliminate dl[I] */
        /* Compute Complex division using nag_complex_divide
        (a02cdc). */
        fact = nag_complex_divide(d[i],dl[i]);
        d[i] = dl[i];
        dl[i] = fact;
        temp = du[i];
        du[i] = d[i+1];
        /* Compute Complex multiply using nag_complex_multiply
        (a02ccc). */
        z1 = nag_complex_multiply(fact,d[i+1]);
        /* Compute Complex subtraction using nag_complex_subtract
        (a02cbc). */
        d[i+1] = nag_complex_subtract(temp,z1);
        du2[i] = du[i+1];
        /* Compute Complex multiply using nag_complex_multiply
        (a02ccc). */
        du[i+1] = nag_complex_multiply(fact,du[i+1]);
        /* Perform Complex negation using nag_complex_negate
        (a02cec). */
        du[i+1] = nag_complex_negate(du[i+1]);
        ipiv[i] = i + 1;
    }
}
if (n > 1)
{
    i = n - 2;
    if (fabs(d[i].re)+fabs(d[i].im) >= fabs(dl[i].re)+fabs(dl[i].im))
    {
        if (fabs(d[i].re)+fabs(d[i].im) != 0.0)
        {
            /* Compute Complex division using nag_complex_divide
            (a02cdc). */
            fact = nag_complex_divide(dl[i],d[i]);
            dl[i] = fact;
            /* Compute Complex multiply using nag_complex_multiply
            (a02ccc). */

```

```

        fact = nag_complex_multiply(fact,du[i]);
        /* Compute Complex subtraction using
           nag_complex_subtract (a02cbc). */
        d[i+1] = nag_complex_subtract(d[i+1],fact);
    }
}
else
{
    /* Compute Complex division using nag_complex_divide
       (a02cdc). */
    fact = nag_complex_divide(d[i],dl[i]);
    d[i] = dl[i];
    dl[i] = fact;
    temp = du[i];
    du[i] = d[i+1];
    /* Compute Complex multiply using nag_complex_multiply
       (a02ccc). */
    z1 = nag_complex_multiply(fact,d[i+1]);
    /* Compute Complex subtraction using nag_complex_subtract
       (a02cbc). */
    d[i+1] = nag_complex_subtract(temp,z1);
    ipiv[i] = i + 1;
}
}
/* Check for a zero on the diagonal of U. */
for (i = 0; i < n; ++i) {
    if (fabs(d[i].re)+fabs(d[i].im) == 0.0)
    {
        *info = i;
        goto END;
    }
}
END:
return;
}

static void my_zgttrs(Integer n, Complex dl[], Complex d[],
                    Complex du[], Complex du2[], Integer ipiv[],
                    Complex b[], Complex y[])
{
    /* A simple C version of the Lapack routine zgttrs with argument
       checking removed, the number of right-hand-sides=1, Trans='N' */
    /* Scalars */
    Complex temp, z1;
    Integer i;
    /* Solve L*x = b. */
    for (i = 0; i < n ; ++i)
    {
        y[i] = b[i];
    }
    for (i = 0; i < n - 1; ++i)
    {
        if (ipiv[i] == i)
        {
            /* y[i+1] = y[i+1] - dl[i]*y[i] */
            /* Compute Complex multiply using nag_complex_multiply
               (a02ccc). */
            temp = nag_complex_multiply(dl[i],y[i]);
            /* Compute Complex subtraction using nag_complex_subtract
               (a02cbc). */
            y[i+1] = nag_complex_subtract(y[i+1],temp);
        }
        else
        {
            temp = y[i];
            y[i] = y[i+1];
            /* Compute Complex multiply using nag_complex_multiply
               (a02ccc). */
            z1 = nag_complex_multiply(dl[i],y[i]);
            /* Compute Complex subtraction using nag_complex_subtract
               (a02cbc). */

```

```

        y[i+1] = nag_complex_subtract(temp,z1);
    }
}
/* Solve U*x = b. */
/* Compute Complex division using nag_complex_divide (a02cdc). */
y[n-1] = nag_complex_divide(y[n-1],d[n-1]);
if (n > 1) {
    /* Compute Complex multiply using nag_complex_multiply
    (a02ccc). */
    temp = nag_complex_multiply(du[n-2],y[n-1]);
    /* Compute Complex subtraction using nag_complex_subtract
    (a02cbc). */
    z1 = nag_complex_subtract(y[n-2],temp);
    /* Compute Complex division using nag_complex_divide (a02cdc). */
    y[n-2] = nag_complex_divide(z1,d[n-2]);
}
for (i = n - 3; i >= 0; --i)
{
    /* y[i] = (y[i]-du[i]*y[i+1]-du2[i]*y[i+2])/d[i]; */
    /* Compute Complex multiply using nag_complex_multiply
    (a02ccc). */
    temp = nag_complex_multiply(du[i],y[i+1]);
    z1 = nag_complex_multiply(du2[i],y[i+2]);
    /* Compute Complex addition using nag_complex_add
    (a02cac). */
    temp = nag_complex_add(temp,z1);
    /* Compute Complex subtraction using nag_complex_subtract
    (a02cbc). */
    z1 = nag_complex_subtract(y[i],temp);
    /* Compute Complex division using nag_complex_divide
    (a02cdc). */
    y[i] = nag_complex_divide(z1,d[i]);
}
return;
}

```

## 9.2 Program Data

nag\_complex\_sparse\_eigensystem\_iter (f12apc) Example Program Data  
 10 4 20 : Vaues for nx, nev and ncv

## 9.3 Program Results

nag\_complex\_sparse\_eigensystem\_iter (f12apc) Example Program Results

The 4 Ritz values of smallest magnitude are:

1	(	34.8720	,	-0.0000	)
2	(	64.4326	,	0.0000	)
3	(	113.6685	,	-0.0000	)
4	(	182.5320	,	0.0000	)

---